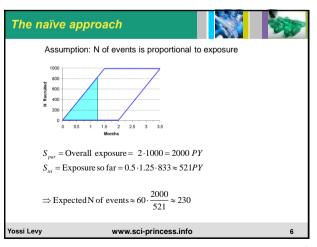
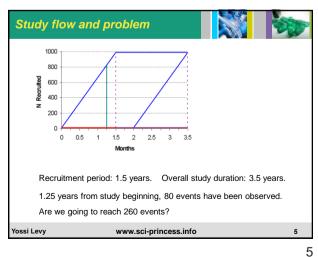


Sample size and power For testing $H_0: \theta = 0$ vs. $H_1: \theta = \theta_R$ $e = \frac{4 \cdot \left(z_{\alpha/2} + z_{\beta}\right)^{2}}{\theta_{p}^{2}}$ The needed number of events is The required sample size is $\alpha = 0.05, 1 - \beta = 0.83, \theta = \log 0.696 \implies e = 260$ $S_C(2) = 0.7 \implies N = 1000$ Yossi Levy www.sci-princess.info

Survival clinical trial Endpoint: time to ("bad") event Two treatment groups: Experimental (E) and Control (C) Fixed treatment duration period of length T 1:1 randomization ratio Proportional hazard ratio assumption - for all t>0: $\theta = -\log[h_E(t)/h_C(t)]$ $= -\log[-\log S_E(t)] + \log[-\log S_C(t)]$ Yossi Levy www.sci-princess.info 3



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Implementation 1* - Whitehead et. al.





- Estimate Ŝ_P(T)
- Solve the system for $\hat{S}_{F}(T)$, $\hat{S}_{C}(T)$:

$$\begin{cases} \hat{S}_{_{E}}(T) = 0.5 \cdot \left[\hat{S}_{_{E}}(T) + \hat{S}_{_{C}}(T) \right] \\ \\ \theta_{_{R}} = -\log \left[-\log \left\{ \hat{S}_{_{E}}(T) \right\} \right] + \log \left[-\log \left\{ \hat{S}_{_{C}}(T) \right\} \right] \end{cases}$$

• Use $\hat{S}_{\scriptscriptstyle E}(T), \ \hat{S}_{\scriptscriptstyle C}(T)$ to estimate the expected number of events at T

*Whitehead et. al. (2001), Statistics In Medicine 20: 165-176

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Whitehead's framework*





- Estimate the overall survivor function from the blinded data
- Construct illustrative survival functions for treatment groups consistent with assumed treatment effect and observed overall survival
- Check whether trial is likely to produce number of events needed

Whitehead emphasizes that the procedure is blinded, since the survival function constructed in the second step "are illustrative survival functions, and not estimates, θ itself has not been estimated from the data and the appropriateness of the proportional hazards model has not been assessed".

But...How is the second step implemented?

*Whitehead (2001). Drug Information Journal, Vol. 35, 1387-1400

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How is the second step implemented?





- Whitehead et. al. (2001) proposed a method that assumes some knowledge (that can be empirical) of S_E(t) and S_C(t)
- Other alternatives assume that each of $S_E(t)$ and $S_C(t)$ depend on a single parameter, λ_E and λ_C , respectively, and that θ can be expressed by these two parameters.
- The exponential survival function and its extension, the Weibull survival function, are examples for such survival function.
- Throughout the rest of the presentation I will use exponential survival for illustration:

$$S_E(t) = e^{-\lambda_E \cdot t}$$
 $S_C(t) = e^{-\lambda_C \cdot t}$ $\theta_R = -\log(\lambda_E/\lambda_C)$

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Implementation 1 (cont.)





- Estimation of $\hat{S}_{p}(T)$
- Suppose mid-review is to be performed at time R (R<T)
- For various $t_i \le R$, i=1,...,k and for t=T, compute $S_P(t_i) = 0.5 \cdot \left[S_F(t_i) + S_C(t_i) \right]$
- Let Φ be the average difference between the anticipated $S_p(t_i)$ and the new $\hat{S}_p(t_i)$ values on the complementary log-log scale for i=1,...,k. That is $\phi = \frac{1}{k} \sum_{i=1}^k \left[-\log \left\{ -\log \hat{S}_p(t_i) \right\} + \log \left\{ -\log S_p(t_i) \right\} \right]$
- Using Φ , estimate $\hat{S}_{p}(T)$ by

$$-\log\left|-\log \hat{S}_p(T)\right| = -\log\left[-\log S_p(T)\right] + \phi$$

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Implementation 3 - estimate λ_{C} from mean time to event





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- Estimate μ_{P_1} the mean time to event in the pooled population
- Solve the set of equations to obtain estimates for λ_{E} and λ_{C}

$$\begin{cases} \mu_P = 0.5 \cdot \left(1/\hat{\lambda}_E + 1/\hat{\lambda}_C \right) \\ \psi = \hat{\lambda}_E / \hat{\lambda}_C \end{cases}$$

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Implementation 2 – estimate λ_C from KM curve





- If that time to event is exponentially distributed, then $S_{\nu}(t) = 0.5 \cdot \left(e^{-\psi \cdot \lambda_C \cdot t} + e^{-\lambda_C \cdot t}\right)$, where $\psi = e^{-\theta}$
- Let $\hat{S}_{p}(t)$ be the pooled Kaplan-Mayer estimator
- Obtain estimates Â_{c,i} by solving for various t_i<=R, (i=1,...,k):

$$\hat{S}_{P}(t_{i}) = 0.5 \cdot \left(e^{-\psi \cdot \lambda_{C} \cdot t_{i}} + e^{-\lambda_{C} \cdot t_{i}} \right)$$

• Estimate λ_C by $\hat{\lambda}_C = \frac{1}{k} \sum_{i=1}^k \hat{\lambda}_{C,i}$

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lmplementation 5 - estimate ג from likelihood of pooled survival?



- Recall that $S_p(t) = 0.5 \cdot \left(e^{-\psi \cdot \lambda_C \cdot t} + e^{-\lambda_C \cdot t} \right)$
- Then the pooled hazard function is

$$\lambda_{p}(t) = \frac{\lambda_{E} \cdot e^{-\lambda_{E} \cdot t} + \lambda_{C} \cdot e^{-\lambda_{C} \cdot t}}{e^{-\lambda_{C} \cdot t} + e^{-\lambda_{C} \cdot t}} = \frac{\psi \cdot \lambda_{C} \cdot e^{-\psi \cdot \lambda_{C} \cdot t} + \lambda_{C} \cdot e^{-\lambda_{C} \cdot t}}{e^{-\psi \cdot \lambda_{C} \cdot t} + e^{-\lambda_{C} \cdot t}}$$

Let t_i be event or censoring time, d_i censoring indicator. Then an MLE for λ_c can be derived from the likelihood function

$$L_{P}(\lambda_{C};(t_{i},d_{i}),i=1,...,N) = \prod_{i=1}^{N} \lambda_{P}(t_{i})^{d_{i}} S_{P}(t_{i})$$

However, this approach is equivalent to the previous one

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lmplementation 4 - estimate ג from mixed likelihood function



If subject i is randomized to group X (X is T or C) then the likelihood for this subject is:

$$L_{i,X}(\lambda_X;t_i,d_i) = \lambda_X(t_i)^{d_i} S_X(t_i)$$

Since it is not known to which group the subject belongs, the likelihood for this subject will be

$$L_{M,i}((\lambda_{P}, \lambda_{E}); t_{i}, d_{i}) = 0.5 \cdot \left[\lambda_{E}(t_{i})^{d_{i}} S_{E}(t_{i}) + \lambda_{C}(t_{i})^{d_{i}} S_{C}(t_{i}) \right]$$

Then the overall likelihood function is

$$L((\lambda_E,\lambda_C)\,;\,(t_i,d_i)\,,\,i=1,\dots,N) = \prod_{i=1}^N 0.5\cdot\lambda_C^{d_i}\cdot \left[\psi^{d_i}\cdot e^{-\lambda_C\psi\cdot t_i} + e^{-\lambda_C\cdot t_i}\right]$$

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Simulation model



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- Time to event ~ Weibull(λ,β)
 - Survival function: $S(t) = \exp\{-(\lambda t)^{\beta}\}$
 - Hazard function $h(t) = \lambda \beta (\lambda t)^{\beta 1}$
- Proportional hazard: $\beta_E = \beta_C = \beta$, $\lambda_E = \lambda_C \cdot \psi^{1/\beta}$

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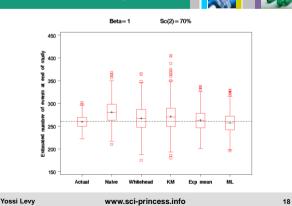
- 2 arm placebo control study: 500 subjects per arm
- Fixed treatment duration: 2 years
- Recruitment period: 1.5 years
- Blinded design review at 1.25 years
- Design review assumptions:
 - Time to event is exponential
 - $S_c(2)=0.7$, $\psi=0.7 => 260$ events are expected

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Simulation results - the good news



Simulation scenarios

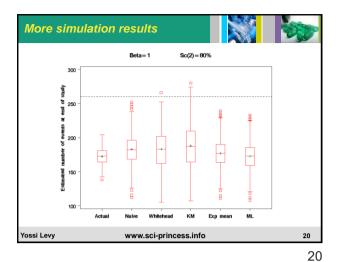


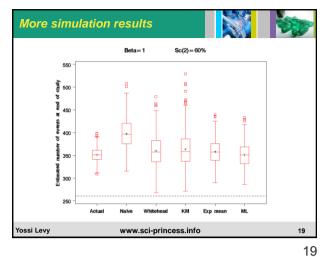


9 scenarios:

- Weibull shape parameter (β):
 - β =0.5 (decreasing hazard)
 - β =1 (constant hazard exponential)
 - β =2 (increasing hazard)
- $S_{C}(2)$ =% of subjects not experiencing event in control group (determining $\lambda_{\rm C}$)
 - 80% (inactive population)
 - 70% (assumed population)
 - 60% (active population)

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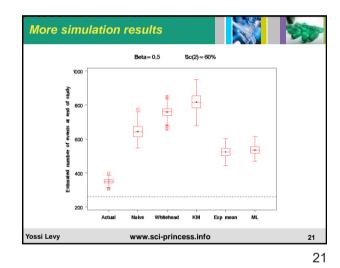
More simulation results

Beta=0.5 Sc(2)=70%

1000

Actual Naive Whitehead KM Exp mean ML

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More simulation results

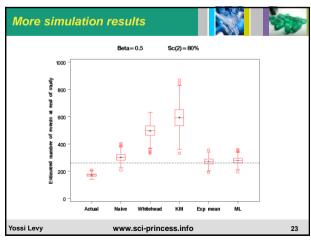
Beta=2 Sc(2)=60%

400

400

Actual Naive Whethead KM Exp mean ML

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